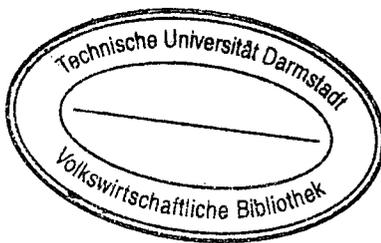


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# Econometric Analysis of Count Data

Third, Revised and Enlarged Edition

With 13 Figures  
and 20 Tables



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