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HANDBOOK OF GAME THEORY

with Economic Applications

VOLUME II

Edited by

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and

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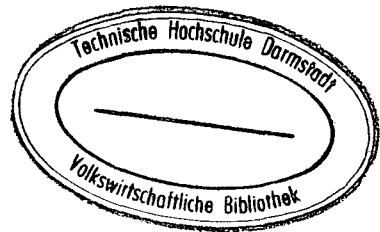
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