

Maintenance Models for Systems subject to Measurable Deterioration

Onderhoudsmodellen voor systemen onderhevig aan meetbare veroudering

PROEFSCHRIFT

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