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**ON THE ESTIMATION OF
STATISTICAL COST
FUNCTIONS**

**AN EMPIRICAL STUDY OF PRODUCTION
AND COST FUNCTIONS OF FINNISH RESTAU-
RANTS**

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