

Essays on Neural Network, Sampling Methods and Instrumental Variables

Essays over neurale netwerken in simulatie methoden
en instrumentele variabelen

PROEFSCHRIFT

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