

Reconstructing Macroeconomics

A Perspective from Statistical Physics and Combinatorial Stochastic Processes

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