

Unconditional and Conditional Modeling of Non-normal Return Densities

with Application to Risk Measurement

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