Why Stock Markets Crash

Critical Events in Complex Financial Systems

D I D I E R S O R N E T T E

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