

# *ECONOMETRICS*

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## *BASIC AND APPLIED*

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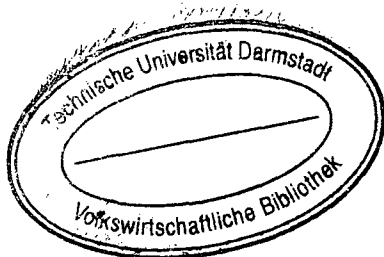
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MACMILLAN PUBLISHING COMPANY

NEW YORK

Collier Macmillan Publishers

LONDON

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