MATHEMATICAL PROGRAMMING:

An Introduction to the Design and Application of Optimal Decision Machines

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