





ACCADEMIA NAZIONALE DEI LINCEI
SCUOLA NORMALE SUPERIORE

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The Theory of Singularities
and Its Applications

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