

**Griffin's Exercises in Statistics and Related Subjects**

**Exercises in  
Mathematical Economics  
and Econometrics  
with Outlines of Theory**



**J. E. Spencer, B.Sc.(Econ.)**

Professor of Economics, The New University of Ulster

**R. C. Geary, D.Sc., D.Econ.Sc.**

Consultant, The Economic and Social Research Institute, Dublin



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