

# AN INTEGRATED SYSTEM OF WORLD MODELS

*with separate models for economic growth,  
population and labour force, energy, food and agriculture,  
machinery and equipment and raw materials*

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