

# Terramechanics

## Land Locomotion Mechanics

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## Preface

Terramechanics is a  
It concerns itself with  
of mobile plant. The  
terrain interaction of  
agricultural vehicle  
of flotation, traffic  
terrains. Within ter  
machine to do effect  
on the physical pro  
characteristics of t  
who are involved in  
mechanical propert  
in the construction  
employed by the op  
by the machinery u  
and land user grou  
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and 'Introduction t  
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to the performance  
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