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## To stop or not to stop

Some Elementary Optimal Stopping Problems with Economic Interpretations

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