

# **Elements of Propulsion: Gas Turbines and Rockets**

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Foreword by

**Hans von Ohain**

German Inventor of the Jet Engine



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**Supporting Material for Chapter 7: Parametric Cycle Analysis for Real Engines**

- SM7.1 Turbofan with Afterburning—Separate Exhaust Systems
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