## Finite Element Techniques for Fluid Flow

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<sup>\*</sup>Topics which may be omitted in an introductory course without affecting continuity.