

# Lecture Notes in Economics and Mathematical Systems

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Mathematical Economics

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## Expectations and Stability in Oligopoly Models

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