

MODEL THEORY FOR INFINITARY LOGIC

LOGIC WITH COUNTABLE CONJUNCTIONS
AND FINITE QUANTIFIERS

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PROBLEMS: End of Lectures 2, 5, 7, 9, 13, 17, 19, 22.