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Editor

Fractal Image Compression

Theory and Application

With 139 Illustrations

Technische Universität Darmstadt
FACHBEREICH INFORMATIK

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