

Lecture Notes in Physics

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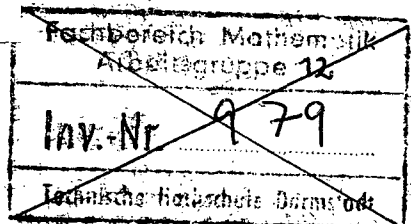
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A Gauge Theory of Dislocations and Disclinations

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