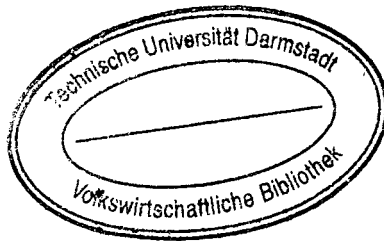


# Introduction to ECONOMETRICS

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# Contents

Preface      *xv*

The Design and Use of This Book      *xvii*

List of Tables      *xxi*

List of Figures      *xxv*

## chapter 1

What Econometrics Is About      *1*

1.1 Typology of Economic Relations      *1*

1.2 The Use of Numerically Specified Economic Relations      *5*

Problems      *5*

**part one**  
**THE SIMPLE REGRESSION MODEL**

**chapter 2**

**Fitting a Straight Line 9**

- 2.1 Data and Theoretical Relations 9
- 2.2 On Sums, Arithmetic Means, and Mean Squares and Products 12
- 2.3 Fitting a Straight Line by Least Squares 17
- 2.4 Some Questions 24

**Problems 25**

**chapter 3**

**Discrete Distribution Theory 27**

- 3.1 Univariate Discrete Distributions 27
- 3.2 Multivariate Discrete Distributions 31
- 3.3 Conditional Distributions and Stochastic Independence 34
- 3.4 The Algebra of Expectations 38

**Problems 40**

**chapter 4**

**Continuous Distribution Theory  
and Statistical Inference 43**

- 4.1 Univariate Continuous Distributions 43
- 4.2 Multivariate Continuous Distribution Theory 46
- 4.3 Statistical Inference 52
- 4.4 Point Estimation 54

**Problems 58**

**chapter 5****Two-Variable Regression 61**

- 5.1 The Standard Linear Model 61
- 5.2 Least Squares Through the Origin 65
- 5.3 Unconstrained Least Squares 70
- 5.4 An Optimal Property of Least-Squares Estimation 78

Problems 82

**chapter 6****Two-Variable Correlation 83**

- 6.1 The Correlation Coefficient of Observation Pairs 83
- 6.2 The Correlation Coefficient of Two Random Variables 85
- 6.3 The Sampling Covariance and Correlation Coefficient  
of the Estimators of Two Parameters 89

Problems 90

**part two****THE MULTIPLE REGRESSION MODEL****chapter 7****Fitting a Plane 95**

- 7.1 Fitting a Plane by Least Squares 96
- 7.2 Extensions 100
- 7.3 Analysis of Residuals 103

Problems 108

**chapter 8**

**Multiple Regression 110**

8.1 Extension of the Standard Linear Model 110

8.2 Least Squares in Multiple Regression 113

8.3 Multicollinearity 121

8.4 Extensions 124

Problems 125

**chapter 9**

**Multiple Correlation 128**

9.1 The Coefficient of Multiple Correlation 128

9.2 The Incremental Contributions of Explanatory Variables 132

9.3 More on Multicollinearity 136

Problems 138

**chapter 10**

**Multivariate Normality and Maximum Likelihood 140**

10.1 The Multivariate Normal Distribution 140

\*10.2 The Method of Maximum Likelihood 147

\*10.3 Maximum-Likelihood Estimation in the Standard Linear Model 149

Problems 151

**chapter 11**

**Confidence and Prediction Intervals 153**

11.1 Two Distributions Associated with the Normal 153

11.2 Confidence Intervals 156

- 11.3 Confidence Intervals in the Standard Linear Model 159  
 \*11.4 Regression Predictions 164  
 Problems 168

## chapter 12

### The Testing of Hypotheses 171

- 12.1 The First Fundamentals of Hypothesis Testing 171  
 12.2 Hypothesis Testing in the Standard Linear Model 174  
 \*12.3 Likelihood Ratio Tests 179  
 Problems 184

## chapter 13

### The Functional Form of a Relation 186

- 13.1 The Meaning of Linearity 186  
 13.2 The Use of Logarithms 188  
 13.3 Dummy Variables 194  
 \*13.4 Linearization 195  
 Problems 197

## chapter 14

### Consumer Demand Equations 200

- 14.1 Introduction to Consumer Demand Theory 200  
 14.2 The Rotterdam Model 207  
 14.3 Statistical Inference in the Rotterdam Model 212  
 \*14.4 Groupwise Extensions --219  
 Problems 226

part three  
EXTENSIONS OF THE REGRESSION MODEL

chapter 15

**Large-Sample Distribution Theory** 231

- 15.1 Introduction to Large-Sample Theory 231
- \*15.2 Large-Sample Analysis 237
- \*15.3 More on Maximum Likelihood 242

Problems 244

chapter 16

**Bayesian Inference  
and Rational Random Behavior** 246

- \*16.1 Bayesian Inference 246
- \*16.2 Bayesian Inference in Econometrics 253
- \*16.3 Rational Random Behavior 255
- \*16.4 The Asymptotic Theory of Rational Random Behavior 258

Problems 265

chapter 17

**Specification and Observational Errors** 267

- 17.1 Functional Forms Further Considered 267
- 17.2 Regression Strategies 273
- 17.3 Specification Analysis 276
- \*17.4 Observational-Errors 281

Problems 285

**chapter 18****Aggregation 288**

- \*18.1 The Specification Approach to the Aggregation Problem 288
- \*18.2 An Extension and an Example 291
- \*18.3 The Convergence Approach to the Aggregation Problem 294

Problems 297

**chapter 19****Generalized Least Squares  
and Related Procedures 299**

- 19.1 Heteroscedasticity and Weighted Least Squares 299
- 19.2 Correlated Disturbances and Autoregressive Transformations 302
- 19.3 Some Statistical Testing Procedures 305
- \*19.4 The Use of Extraneous Estimators 308
- \*19.5 Mixed Estimation 311

Problems 316

**chapter 20****Introduction to Simultaneous-Equation Problems:  
Static Equation Systems 319**

- 20.1 Endogenous and Exogenous Variables 319
- 20.2 Structural Equations and the Reduced Form 321
- 20.3 Least Squares, Indirect Least Squares, and  
Instrumental Variables 323
- 20.4 The Identification Problem 326
- 20.5 Two-Stage Least Squares 328

Problems 330



**chapter 21**

**Dynamic Equation Systems 332**

- 21.1 Distributed Lags 332
- 21.2 An Example of a Dynamic Equation System 334
- 21.3 Identification and Estimation in Dynamic Equation Systems 340
- 21.4 The Final Form of a Dynamic Equation System 342
- \*21.5 Recursive Systems 346
- \*21.6 Extensions 349

Problems 352

**part four**

**PREDICTION AND CONTROL**

**chapter 22**

**The Evaluation of Economic Predictions 359**

- 22.1 Predictions and Prediction Errors 359
- 22.2 Predicting the Future and Estimating the Past 362
- 22.3 Mean-Square-Error Analysis of Predictions and Estimates 365
- 22.4 Some Useful Diagrams 370

Problems 375

**chapter 23**

**Prediction and Control 377**

- \*23.1 Typology of Predictions 377
- \*23.2 Predictions Based on Econometric Models 380
- \*23.3 Some Problems of Optimal Control 384

Problems 395

**Appendix      396**

- A Least-Squares Adjustment in Matrix Notation 396
- B Least-Squares Estimation in Matrix Notation 399
- C The Normal and Associated Distributions 403
- D The Slutsky Matrix 405
- E Rational Random Behavior 413
- F Aggregation 416
- G Generalized Least Squares 418
- H Two-Stage Least Squares 421

**Problems      424****References      427****Statistical Tables      433****Index      443**