

MOLECULAR SPECTRA *and* MOLECULAR STRUCTURE

III. ELECTRONIC SPECTRA AND ELECTRONIC STRUCTURE OF POLYATOMIC MOLECULES

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