

# **A Programming Approach to Computability**

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\* These sections may be omitted with no loss of continuity.