

Heft 132 Finite Volume Models
for Multiphase Multicomponent
Flow through Porous Media

von
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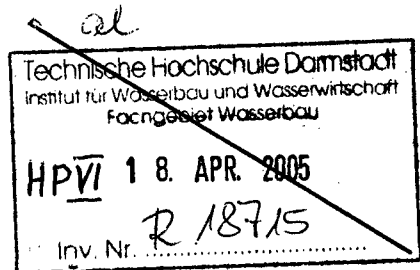


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