

# Lecture Notes in Economics and Mathematical Systems

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Christoph Klein

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A Static Microeconomic Model  
of Pure Competition

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