

**Institut für Wasserbau und Wasserwirtschaft**  
**Technische Universität Darmstadt**



**„A Contribution to the Uncertainty Analysis of Distributed Hydrological Models“**

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