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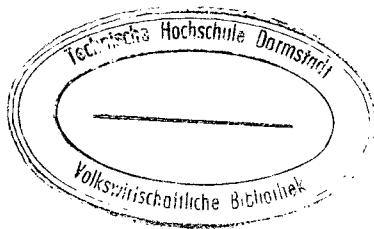
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LARGE SAMPLE ESTIMATION AND HYPOTHESIS TESTING*

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