# Fluid Mechanics and Thermodynamics of Turbomachinery

Fourth Edition, in SI/Metric units

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Boston Oxford Johannesburg Melbourne New Delhi Singapore

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