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## Optimal Control Allocation for Road Vehicle Dynamics using Wheel Steer Angles, Brake/Drive Torques, Wheel Loads and Camber Angles

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