THIRD EDITION

THE STRUCTURE OF ECONOMICS

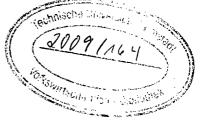
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A MATHEMATICAL ANALYSIS

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CONTENTS

vii

Preface	xv
Comparative Statics and the Paradigm of Economics	1
Introduction	1
The Marginalist Paradigm	3
Theories and Refutable Propositions	9
The Structure of Theories	10
Refutable Propositions	12
Theories Versus Models; Comparative Statics	14
Examples of Comparative Statics	16
Problems	23
Selected References	24
Bibliography	24
Review of Calculus (One Variable)	25
Functions, Slopes, and Elasticity	25
Maxima and Minima	27
Continuous Compounding	28
The Mean Value Theorem	31
Taylor's Series	32
Applications of Taylor's Series: Derivation of the First- and Second- Order	
Conditions for a Maximum; Concavity and Convexity	34
Functions of Several Variables	37
Functions of Several Variables	37
	37
Partial Derivatives	39
	Comparative Statics and the Paradigm of Economics Introduction The Marginalist Paradigm Theories and Refutable Propositions The Structure of Theories Refutable Propositions Theories Versus Models; Comparative Statics Examples of Comparative Statics Problems Selected References Bibliography Review of Calculus (One Variable) Functions, Slopes, and Elasticity Maxima and Minima Continuous Compounding The Mean Value Theorem Taylor's Series Applications of Taylor's Series: Derivation of the First- and Second- Order Conditions for a Maximum; Concavity and Convexity Functions of Several Variables Functions of Several Variables Level Curves: 1

viii contents

3.4	The Chain Rule	4.5
	Second Derivatives by the Chain Rule	47
3.5	Level Curves: II	49
	Convexity of the Level Curves	5
	Monotonic Transformations and Diminishing Marginal Utility	53
	Problems	55
3.6	Homogeneous Functions and Euler's Theorem	56
	Problems	6.5
	Selected References	65
4	Profit Maximization	60
4.1	Unconstrained Maxima and Minima: First-Order Necessary Conditions	66
4.2	Sufficient Conditions for Maxima and Minima: Two Variables	68
7.4	Problems	72
4.3	An Extended Footnote	73
4.4	An Application of Maximizing Behavior: The Profit-Maximizing Firm	74
	The Supply Function	81
4.5	Homogeneity of the Demand and Supply Functions; Elasticities	82
1	Elasticities	83
c4:6	The Long Run and the Short Run: An Example of the Le Châtelier Principle	84
	A More Fundamental Look at the Le Châtelier Principle	86
	Problems	83
4.7	Analysis of Finite Changes: A Digression	9:
	Appendix	92
	Taylor Series for Functions of Several Variables	92
	Concavity and the Maximum Conditions	93
	Selected References	95
5	Matrices and Determinants	90
5.1	Matrices	
5.1	Determinants, Cramer's Rule	90 98
5.3	The Implicit Function Theorem	10:
5.5	Problems	10.
	Appendix	110
	Simple Matrix Operations	110
	The Rank of a Matrix	112
	The Inverse of a Matrix	113
	Orthogonality	113
	Problems	110
	Selected References	110
6	Comparative Statics: The Traditional Methodology	117
6.1	Introduction; Profit Maximization Once More	111
6.2	Generalization to <i>n</i> Variables	12
0.2	First-Order Necessary Conditions	12
	Second-Order Sufficient Conditions	12
	Profit Maximization: n Factors	124

6.3	The Theory of Constrained Maxima and Minima: First-Order	
	Necessary Conditions	128
6.4	Constrained Maximization with More than One Constraint: A Digression	132
6.5	Second-Order Conditions	134
	The Geometry of Constrained Maximization	138
6.6	General Methodology	141
	Problems	148
	Selected References	150
7	The Envelope Theorem and Duality	151
7.1	History of the Problem	151
7.2	The Profit Function	152
7.3	General Comparative Statics Analysis: Unconstrained Models	156
7.4	Models with Constraints	159
	Comparative Statics: Primal-Dual Analysis	161
	An Important Special Case	165
	Interpretation of the Lagrange Multiplier	166
	Le Châtelier Effects	169
	Problems	172
بَرَ مِع	≆Bibliography	174
8	The Derivation of Cost Functions	175
8.1	The Cost Function	175
8.2	Marginal Cost	179
8.3	Average Cost	180
8.4	A General Relationship Between Average and Marginal Costs	181
8.5	The Cost Minimization Problem	183
8.6	The Factor Demand Curves	189
	Interpretation of the Lagrange Multiplier	189
8.7	Comparative Statics Relations: The Traditional Methodology	193
8.8	Comparative Statics Relations Using Duality Theory	202
	Reciprocity Conditions	202
	Cost Curves in the Short and Long Run	205
	Factor Demands in the Short and Long Run	207
0.0	Relation to Profit Maximization	209
8.9	Elasticities; Further Properties of the Factor Demand Curves	211
	Homogeneity	212
0.10	Output Elasticities	216
	The Average Cost Curve	216
8.11	Analysis of Firms in Long-Run Competitive Equilibrium	218
	Analysis of Factor Demands in the Long Run	220
	Problems Selected References	222 224
		224
9	Cost and Production Functions: Special Topics	225
9.1	Homogeneous and Homothetic Production Functions	225
2,2	The Cost Function: Further Properties	228
	Homothetic Functions	232

X CONTENTS

9.3	The Duality of Cost and Production Functions	234
	The Importance of Duality	237
9.4	Elasticity of Substitution; the Constant-Elasticity-of-Substitution (CES)	
	Production Function	238
	Generalizations to n Factors	248
	The Generalized Leontief Cost Function	249
	Problems	250
	Bibliography	250
10	The Derivation of Consumer Demand Functions	252
10.1	Introductory Remarks: The Behavioral Postulates	252
10.2	Utility Maximization	261
	Interpretation of the Lagrange Multiplier	266
	Roy's Identity	268
10.3	The Relationship Between the Utility Maximization Model and the Cost	
	Minimization Model	272
10.4	,	
	Derivation of the Slutsky Equation	276
10.5	7 1	282
	Conditional Demands	286
	The Addition of a New Commodity	288
10.6	·	
	Real-Income-Held-Constant Demand Curves	291
	The Slutsky Equation in Elasticity Form	291
10.5	Compensated Demand Curves	294
10.7	1 1	297
	Separable Utility Functions	297
	The Labor-Leisure Choice	299
	Slutsky Versus Hicks Compensations	304
	The Division of Labor Is Limited by the Extent of the Market	306
	Problems Selected References	310 313
	Selected References	313
11	Special Topics in Consumer Theory	314
11.1	8	314
11.2	2	322
	Integrability	325
11.3	1	332
	Shipping the Good Apples Out	335
11.4		341
	Comparative Statics	345
11.5	I	347
	Example	354
	Empirical Approximations	355
11.6		357
	Linear Expenditure System	357
	CES Utility Function	359
	Indirect Addilog Utility Function	360

		CONTENTS	хi
	Translog Specifications		361
	Almost Ideal Demand System		362
	Problems		363
	References on Theory		366
	References on Functional Forms		366
12	Intertemporal Choice		368
12.1	n-Period Utility Maximization		368
	Time Preference		371
	Fisherian Investment		378
	The Fisher Separation Theorem		380
	Real Versus Nominal Interest Rates		382
12.2	The Determination of the Interest Rate		384
12.3	Stocks and Flows		387
	Problems		391
	Selected References		392
13	Behavior Under Uncertainty		394
13.1	Uncertainty and Probability		394
مُنْ يَرُ	Random Variables and Probability Distributions		395
	Mean and Variance		396
13.2	Specification of Preferences		399
	State Preference Approach		399
	The Expected Utility Hypothesis		400
	Cardinal and Ordinal Utility		401
13.3	Risk Aversion		403
	Measures of Risk Aversion		405
	Mean-Variance Utility Function		406
	Gambling, Insurance, and Diversification		409
13.4	Comparative Statics	·	411
	Allocation of Wealth to Risky Assets		411
	Output Decisions Under Price Uncertainty		412
	Increases in Riskiness		413
	Problems		416
	Selected References		416
14	Maximization with Inequality and		
	Nonnegativity Constraints		418
14.1	Nonnegativity		418
	Functions of Two or More Variables		423
14.2	Inequality Constraints		427
14.3	The Saddle Point Theorem		432
14.4	Nonlinear Programming		437
14.5	An "Adding-Up" Theorem		440
	Problems		442
	Appendix		443
ď	Bibliography		446

15	Contracts and Incentives	448
15.1	The Organization of Production	448
15.2	Principal-Agent Models	449
	Comparative Statics	452
	Multitask Agency	454
15.3	Performance Measurement	457
	Choosing the Performance Measure	460
15.4	Costly Monitoring and Efficiency Wages	461
15.5	Team Production	463
15.6	•	466
	Factors Affecting Ownership Structure	469
	Problems	471
	Selected References	471
16	Markets with Imperfect Information	473
16.1	The Value of Information in Decision Making	473
16.2	Search	474
	Sequential Search	476
	Equilibrium Price Dispersion	478
16.3	Adverse Selection	482
	Favorable Selection	485
16.4	Signaling	487
	A More General Analysis	490
16.5	Monopolistic Screening	491
	Problems	496
	Selected References	497
, 17	General Equilibrium I: Linear Models	498
¹ 17.1	Introduction: Fixed-Coefficient Technology	498
17.2	The Linear Activity Analysis Model: A Specific Example	507
17.3	The Rybczynski Theorem	513
17.4	The Stolper-Samuelson Theorem	515
17.5	The Dual Problem	517
17.6	The Simplex Algorithm	526
	Mathematical Prerequisites	526
	The Simplex Algorithm: Example	530
	Problems	534
	Bibliography	536
18	General Equilibrium II: Nonlinear Models	537
18.1	Tangency Conditions	537
18.2	General Comparative Statics Results	545
18.3	The Factor Price Equalization and Related Theorems	550
	The Four-Equation Model	550
	The Factor Price Equalization Theorem	558
	The Stolper-Samuelson Theorems	559
	The Rybczynski Theorem	566

	CONTENTS	xiii
18.4	Applications of the Two-Good, Two-Factor Model	568
18.5	Summary and Conclusions	572
10.0	Problems	574
	Bibliography	576
19	Welfare Economics	577
19.1	Social Welfare Functions	577
19.2	The Pareto Conditions	581
	Pure Exchange	581
	Production	584
19.3	The Classical "Theorems" of Welfare Economics	591
19.4	A "Nontheorem" About Taxation	594
19.5	The Theory of the Second Best	595
19.6	Public Goods	597
19.7	Consumer's Śurplus as a Measure of Welfare Gains and Losses	600
19.8	Property Rights and Transactions Costs	604
	The Coase Theorem	608
	The Theory of Share Tenancy: An Application of the Coase Theorem	611
	Problems	615
A.	æBibliography	616
20	Resource Allocation over Time: Optimal Control Theory	617
20.1	The Meaning of Dynamics	617
	Brief History	621
20.2	Solution to the Problem	621
	The Calculus of Variations	627
	Endpoint (Transversality) Conditions	629
	Autonomous Problems	630
	Sufficient Conditions	632
20.3	Solutions to Differential Equations	633
	Simultaneous Differential Equations	636
20.4	Interpretations and Solutions	637
	Intertemporal Choice	637
	Harvesting a Renewable Resource	640
	Capital Utilization	644
	Problems	649
	Selected References	650
	Hints and Answers	652
	İndex	661

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