

# Lecture Notes in Economics and Mathematical Systems

Managing Editors: M. Beckmann and W. Krelle

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FB Mathematik TUD



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An Inter-Industry  
Translog Model of Prices  
and Technical Change  
for the West German Economy



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