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# Control of Fuel Cell Power Systems

**Principles, Modeling, Analysis and  
Feedback Design**

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With 111 Figures



Springer

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