## Lecture Notes in Economics and Mathematical Systems

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**Economic Theory** 

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## Information Structures in Economics

Studies in the Theory of Markets with Imperfect Information



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