

P.K. Rastogi (Ed.)

# Holographic Interferometry

*Principles and Methods*

With 178 Figures, Some in Colour

Springer-Verlag

Berlin Heidelberg New York London Paris

Tokyo Hong Kong Barcelona Budapest

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