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# Lecture Notes in Economics and Mathematical Systems

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# On the Use of Stochastic Processes in Modeling Reliability Problems

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