

Lecture Notes in Economics and Mathematical Systems

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Operations Research

172

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GERT Networks

and the Time-Oriented Evaluation of Projects



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CONTENTS

List of Symbols	8
Summary of Assumptions	10
Chapter 1 Basic Concepts	11
1.1 Directed Graphs and Activity Networks	11
1.2 GERT Networks	18
1.3 Assumptions Required for GERT Networks	25
1.4 Evaluation of GERT Networks	30
1.5 Subnetworks of GERT Networks	37
Chapter 2 STEOR Networks	45
2.1 Stochastic Processes Connected with STEOR Networks	45
2.1.1 STEOR Networks and MARKOV Renewal Processes	45
2.1.2 GERT Networks with Only EOR Nodes	49
2.2 The MRP Method for the Evaluation of STEOR Networks	53
2.2.1 The Activation Functions and Activation Numbers	53
2.2.2 Special Cases and Examples	59
2.3 The Numerical Implementation of the MRP Method	65
2.4 The MASON Rule	75
2.5 Earliest and Latest Times in STEOR Networks	82
2.6 Applications	93
2.6.1 Time Planning for R&D Projects	94
2.6.2 Production Planning	98
2.6.3 Legislation and Administration of Justice	101
2.6.4 Evaluation of Linear Transmission Systems	103
2.6.5 Description and Analysis of Queueing Models	108
Chapter 3 GERT Networks with Basic Element Structures	116
3.1 Nodes Which Belong Together	117
3.2 Basic Elements	120
3.3 Basic Element Structures	124
3.3.1 Definition and Properties of a Basic Element Structure	124
3.3.2 BES Networks	129
3.3.3 Examples	137
3.4 Evaluation of Admissible Basic Element Structures	140

3.5 Determination of Admissible Interior Basic Element Structures	146
3.5.1 Determination of Nodes Belonging Together (Labeling Process)	147
3.5.2 Construction of a Possible Interior Basic Element Structure	149
3.5.3 Testing of a Possible Interior Basic Element Structure	153
3.5.4 The BES Method	156
3.6 Applications	160
3.6.1 Rendezvous of Two Space Vehicles	161
3.6.2 Production of a Television Program	161
3.6.3 Introduction of a New Industrial Product	167
3.6.4 Reliability Problems	169
Chapter 4 Evaluation of General GERT Networks	172
4.1 Cycle Reduction	172
4.2 Evaluation of an Acyclic GERT Network N	175
4.2.1 Construction of the Sequence (N^H) of Subnetworks of N	177
4.2.2 Determination of the Conditional Probabilities in (4.2.2)	180
4.2.3 Test of the Assumptions A6 and A7	186
4.2.4 Example	187
4.3 Applications	193
4.3.1 Construction of a Turbine	193
4.3.2 Development of a Camera	196
4.4 Replacement of Non-genuine IOR Nodes	199
Chapter 5 Multiple Activations of Non-STEOR Nodes	204
5.1 Generalized GERT Networks and Closed Subnetworks	204
5.2 Assumptions Required for Generalized GERT Networks	208
5.3 Evaluation of Generalized GERT Networks	212
5.3.1 A Method for Evaluating Admissible Generalized GERT Networks	212
5.3.2 Test of the Assumptions for a Generalized GERT Network	214
5.4 Applications	215
5.4.1 Introduction of a New Product	215
5.4.2 Overhaul of a Generator	218
Chapter 6 GERT Networks with Time-dependent Arc Weights	220
6.1 Basic Concepts	220
6.2 STEOR Networks	222
6.3 GERT Networks with Basic Element Structures	225
6.4 General GERT Networks	231

Contents	7
Chapter 7 Simulation	233
7.1 GERTS Networks and Equivalent GERT Networks	233
7.2 GERTS Networks Which Do Not Have Corresponding GERT Networks	236
7.3 Simulation of GERTS Networks	238
7.4 Generalized GERTS Networks	242
7.5 A Universal Method for Evaluating Admissible GERT Networks	244
Appendix	250
A.1 Some Formulas from Probability Theory	250
A.2 Stochastic Processes	252
A.3-Precise Formulation of Assumption A3	257
References	260
Index	262