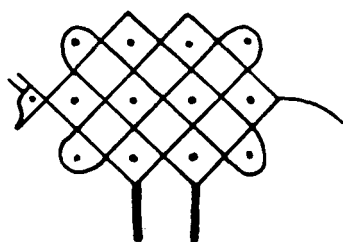


*Companion Encyclopedia
of the
History and Philosophy
of the
Mathematical Sciences*

Volume 1

Edited by
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