

# Lecture Notes in Economics and Mathematical Systems

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Operations Research

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## Redundancy in Mathematical Programming

A State-of-the-Art Survey

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