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Economic Theory of Fuzzy Equilibria

An Axiomatic Analysis

Second, Revised and Enlarged Edition





Contents

Acknowledgements										
Preface to the 1st Edition ix										
Preface to the 2nd Edition xiii										
General Introduction 1										
1	Indi	ndividual Fuzzy Relation of Preference								
	1.1	The F	uzzy Binary Relation of Preference	6						
		1.1.1	Binary Relation and Fuzzy Binary Relation	6						
		1.1.2	The Fuzzy Preference and its Properties	8						
	1.2	The Ir	ndifference Paradox	15						
		1.2.1	Reflexivity and Indifference	15						
		1.2.2	The Axiomatic Solution	16						
		1.2.3	Solution	17						
	1.3	Fuzzy	Utility Function on a Countable Set	18						
		1.3.1	Subrelations of Similitude	19						
		1.3.2	The Transition Operator	19						
		1.3.3	Utility and Fuzzy Reflexivity	20						
		1.3.4	Totally Ordered Fuzzy Topological Space	20						
		1.3.5	A Fuzzy Utility Function	21						
	1.4	Fuzzy	Utility Function on a Convex Set	23						
		1.4.1	Assumptions on X	23						
		1.4.2	The Associated Fuzzy Set X_f	23						
		1.4.3	Analysis of Assumptions	23						
		1.4.4	Continuity of Fuzzy Preferences	24						
		1.4.5	Assumption of Continuity for Fuzzy Preferences	24						
		1.4.6	Preliminary Results	25						
		1.4.7	Extension of $v(x)$ to $u(x)$ on $X \ldots \ldots \ldots \ldots$	27						
	1.5	A Nev	v Proof for Fuzzy Utility	28						
		1.5.1	New Definitions and Notations	29						
		1.5.2	Two Representation Lemmas	30						

-

		1.5.3	A Third Representation Theorem	32			
		1.5.4	Some Concluding Remarks	33			
2	Agg	Aggregation of Fuzzy Preferences					
	2.1	Arrov	ian Dictator and Fuzzy Preferences	36			
		2.1.1	Imprecise Behavior and Fuzzy Individual Preferences .	37			
		2.1.2	Fuzzy Preferences and Collective Decision : Arrow's				
			Axioms	39			
		2.1.3	Proof of the Dictator Theorem with Fuzzy Preferences	42			
	2.2	Fuzzy	Coalitions and Democracy	43			
		2.2.1	Axioms of May's Theorem	44			
		2.2.2	Generalized Theorem : Arrow versus May	52			
A	nnex	es		57			
3	Fuz	zy Ga	mes	63			
	3.1	Fixed	Points and Nash-Equilibrium	64			
		3.1.1	Fixed Points and Fuzzy Universe	65			
		3.1.2	Nash-Equilibria for Fuzzy Games	68			
	3.2	Prude	nt Behavior and Equilibria	78			
		3.2.1	Lexicographic Preorder and Continuity	79			
		3.2.2	Noncooperative Fuzzy Ordinal Game	83			
		3.2.3	Strategic Utility Function	84			
		3.2.4	Prudent Equilibria and Fuzzy Nash-Equilibria	85			
	3.3 Cooperative Fuzzy Games		erative Fuzzy Games	88			
		3.3.1	f-Convexity and Fuzzy Preorders	89			
		3.3.2	Nonemptiness of the Peripheral Core	93			
4	Fuz	Fuzzy General Equilibrium					
	4.1	Tasks	and Quasi Wage-Rates	106			
		4.1.1	The Different Approaches of Ability	106			
		4.1.2	Task, Quasi Wage-Rate and Partial Competition	107			
		4.1.3	A Labor-Commodities-Economy	108			
		4.1.4	A Fuzzy LCE	110			
		4.1.5	The Method for Fuzzy Optimization	112			
	4.2	The E	xistence of a Fuzzy General Equilibrium	115			
		4.2.1	A Private Ownership LCE	116			
		4.2.2	A General Fuzzy Equilibrium (à la Ponsard)	116			
		4.2.3	Existence of Equilibria for a LCE à la Ponsard	119			
		4.2.4	Existence of a General Equilibrium in a Pure LCE .	120			
5	Unc	leremj	ployment Fuzzy Equilibrium	123			
•	5.1	Existe	nce of an Underemployment Equilibrium	124			
		5.1.1	Voluntary Unemployment and Walrasian Equilibrium				
			Involuntary Unemployment	124			

٠

		The Consumer-Worker's Behavior	126						
		5.1.3	General Model of a Pure LCE	129					
	5.2	Involu	ntary Unemployment and Dominated Irrationality	134					
		5.2.1	Preliminary Remarks	135					
		5.2.2	Fuzzy Preference and Involuntary Unemployment	136					
		5.2.3	The Walrasian Equilibrium Involuntary Unemployed						
			Worker's Behavior	139					
		5.2.4	Voluntary and Involuntary Unemployed Workers	140					
6	Fuzzy Economics : An Overview								
	6.1	The B	irth of RPA	145					
	6.2	Preference Theory within RPA							
	6.3	Towards a Fuzzy Theory of Value							
	6.4	RPB a	and RPC Instrumentalism	150					
	6.5	Outlet	s for \mathbb{RP}	151					
G	General Conclusion								
References									
Index									

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