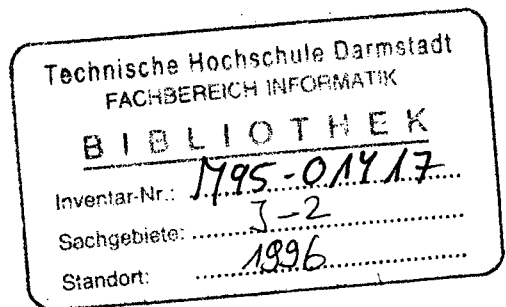


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# Spatial Representation and Motion Planning



Springer

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