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Monte Carlo Simulation in Statistical Physics

An Introduction

With 34 Figures

Physikalische Bibliothek

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