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Non-Standard Computation

Molecular Computation – Cellular Automata – Evolutionary Algorithms – Quantum Computers

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Inventar Nr. PC / M 703

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