## A Game Theory Analysis of Options

Contributions to the Theory of Financial Intermediation in Continuous Time





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