INTUITIONISM AND PROOF THEORY
PROCEEDINGS OF THE SUMMER CONFERENCE AT BUFFALO N.Y. 1968

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* Prof. Yessenin-Volpin was invited to give the opening address, and submitted the paper herein printed as I. However he was unfortunately unable to attend, and Prof. Heyting read the paper VI as an opening address.

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† Bernays was unfortunately unable to attend, and so his paper XXV was read by Howard