

# CONTINUUM MECHANICS

Concise Theory and Problems

Second Corrected and Enlarged Edition

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### *Note to the reader*

In each chapter equations to which subsequent reference is made are numbered from (1). Equation (43) of Chapter 1 is referred to as (43) *in that chapter*: in the later chapters it is referred to as (1.43). The same convention applies in references to sections, problems, exercises and figures.