

# **Avoidance of brake squeal by a separation of the brake disc's eigenfrequencies: A structural optimization problem**

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