

# Statistical estimation of linear economic relationships

Distributed lags and  
simultaneous equations

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