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Concepts and Models of a
Quantitative Sociology

The Dynamics of Interacting Populations

With 71 Figures

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Contents

1. Introduction and Outline	1
1.1 Synergetic Concepts in the Natural Sciences	1
1.1.1 Physico-Chemical Systems	2
1.1.2 Dynamics and Equations of Motion in Physico-Chemical Systems	3
1.2 Synergetic Concepts in Sociology	10
1.3 Significance and Limitations of Quantitative Sociology	14
2. Opinion Formation – an Elementary Example of Semi-Quantitative Sociology	18
2.1 The Model	18
2.2 The Equations of Motion	19
2.2.1 The Master Equation for $p(n; t)$	19
2.2.2 The Fokker-Planck Equation for $P(x; t)$	22
2.2.3 The Langevin Equation for $x(t)$	25
2.2.4 Equations for Mean Values	26
2.3 Solutions of the Equations of Motion	28
2.3.1 Stationary Solutions	28
2.3.2 *Time Dependent Solutions	30
2.4 Choice of Transition Probabilities and the Explicit Form of the Model	40
2.5 The Sociological Interpretation of the Model	45
3. Fundamental Concepts of Quantitative Sociology	55
3.1 Attitude Space, Socio-Configuration and Situation Space	55
3.2 Equations of Motion for the Socio-Configuration	58
3.2.1 The Master Equation	58
3.2.2 The Stochastic and the Fokker-Planck Equation	62
3.2.3 *The Langevin Equations and the Fokker-Planck Equation	66
3.2.4 Approximate Mean Value Equations	72
3.2.5 *Exact Mean Value Equations	73
3.3 The Dynamics of Trend Parameters and of the Situation Vector	76
3.4* Mean Value Equations for Grossvariables of the Socio-Configuration	78

	Contents	XI
4. Migration and/or Birth-Death Processes in Populations		86
4.1 *The General Model		87
4.2 Migration of Two Interacting Populations Between Two Parts of a City		90
4.2.1 Master Equation, Mean Value, Variance and Fokker-Planck Equations		91
4.2.2 Solutions of the Equations in Relevant Cases		96
4.3 Birth-Death Processes Within a Single Population		112
4.3.1 Stochastic Versus Deterministic Description		112
4.3.2 *Multi-Step Birth-Death Processes		122
4.4 Migration and Predator-Prey Interaction Between Two Species		127
4.4.1 Master Equation and Mean Value Equations for the Special Model		128
4.4.2 Comparison of Predator-Prey Interaction Without and With Non-Linear Migration		131
5. Non-Equilibrium Theory of Investment: "The Schumpeter Clock"		141
5.1 Introduction		141
5.1.1 The Relation to Preceding Concepts and Models		141
5.1.2 The Purpose, the Main Proposition and the Limitations of the Schumpeter Clock Model		142
5.2 Macro- and Micro-Economic Variables of the Model and Their Interdependence		143
5.2.1 Strategic Investment		143
5.2.2 The Investors' Configuration		145
5.2.3 Strategic Investment and the Investors' Configuration		147
5.3 Design of the Investors' Interaction Model		148
5.3.1 The Equation of Motion for the Investors' Configuration		149
5.3.2 The Equation of Motion for the Investors' Propensities		155
5.3.3 The Closed Set of Equations of Motion		157
5.4 Structural Analysis of the System of Equations		158
5.4.1 The Singular Points of the Equations of Motion		158
5.4.2 Stability Analysis		159
5.4.3 The Limit Cycle Existence Theorem		161
5.5 Numerical Analysis Based on the Model		164
5.5.1 Model Solutions for the Motion of a Hypothetical Economy in Ideal Time		164
5.5.2 Changes in Industrial Strategic Investment in the Federal Republic of Germany Between 1956 and 1978		168
6. The Interaction of Competitive Macrosocieties		175
6.1 Reconsideration of the Problem of Model Construction		175
6.2 The "Minimal Model"		178
6.2.1 The Grossvariables of the Model		178
6.2.2 The Equations of Motion		182

XII Contents

6.3 Solutions of the Model Equations	193
6.3.1 Stationary Solutions	194
6.3.2 Numerical Analysis of Non-Stationary Solutions	195
6.4 Political Implications	204
References	209
Subject Index	214