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Concepts and Models of a Quantitative Sociology

The Dynamics of Interacting Populations

With 71 Figures

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