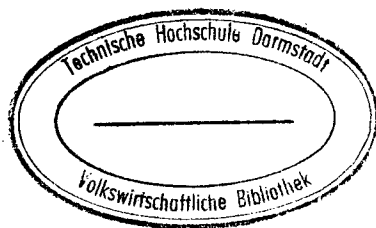


Nonlinear Preference and Utility Theory

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WHEATSHEAF BOOKS

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